

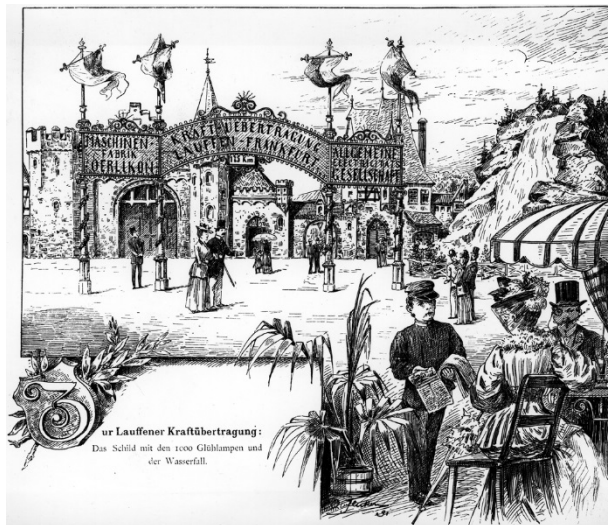
# **DAT300**

# **THE ELECTRICAL POWER SYSTEM**

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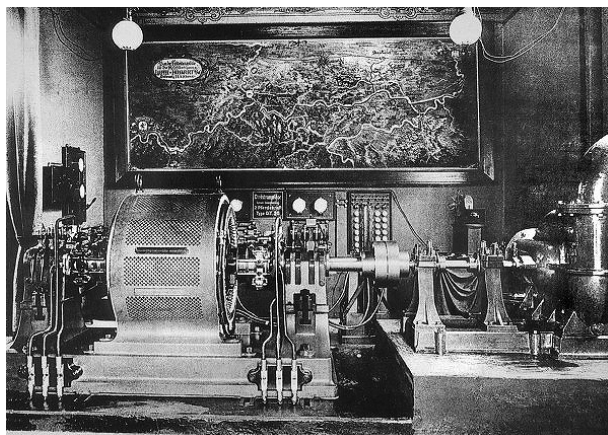
**Department of Electrical Engineering**  
**Division of Electric Power Engineering**  
**Chalmers University of technology**

# History of the power systems



AC transmission was first demonstrated at an exhibition in Frankfurt am Main 1891

170 kW transferred 175 km from Lauffen hydropower station to the exhibition area at 13000-14700 V



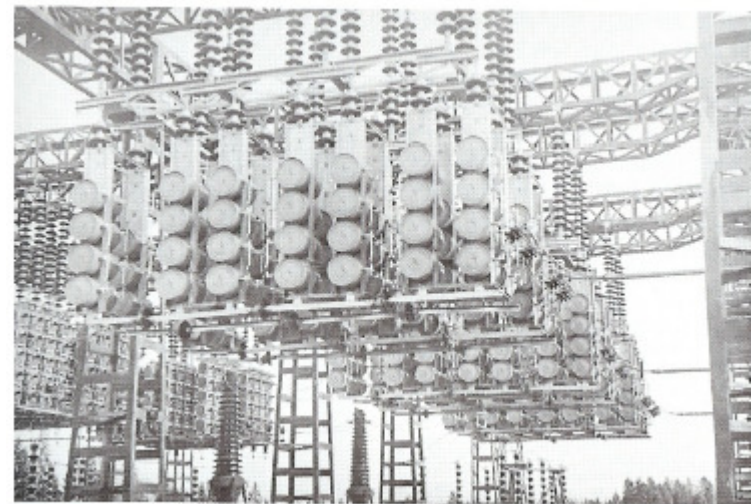
# History of the power systems in Sweden



First 3-phase transmission system  
installed in Sweden between Hellsjön  
and Grängesberg 1893  
voltage 9650 V, 70 Hz, 70 kW

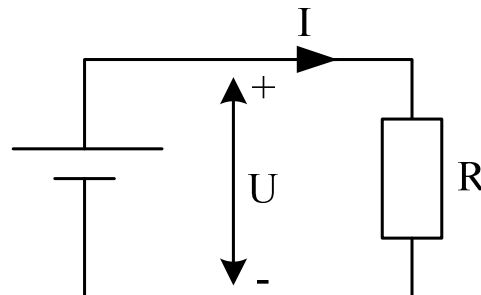
First 400 kV system Harsprånget  
Hallsberg 1952

Series compensation introduced  
1954

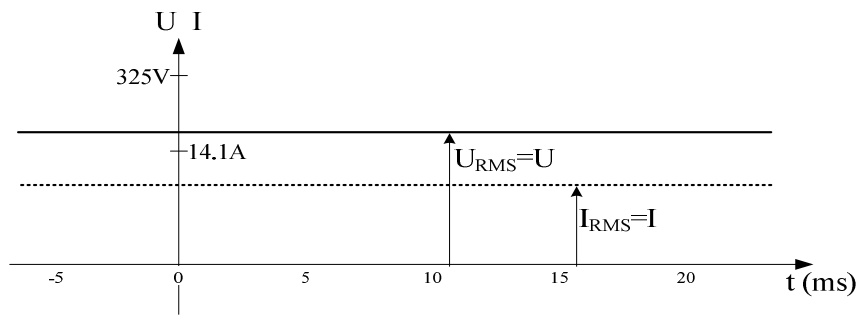
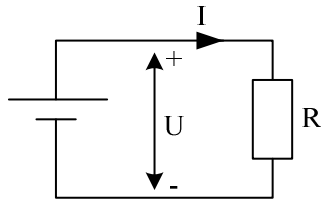


# Fundamentals of Electric Power

- Energy
  - Ability to perform work, [J], [Ws], [kWh] (1 kWh = 3.6 MJ)
  
- Voltage
  - Measured between two points [V], [kV]
  - Equivalent to pressure in a water pipe
  
- Current
  - Measure of rate of flow of charge through a conductor [A], [kA]
  - Equivalent to the rate of flow of water through a pipe.
  - Must have a closed circuit to have a current

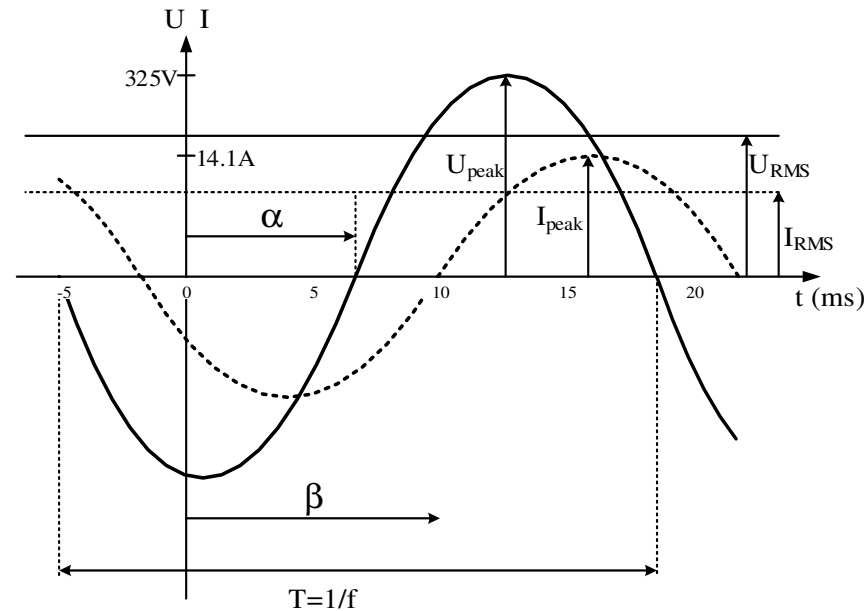
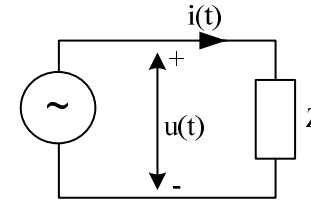


# Direct Current (DC) / Alternating Current (AC)



$$u(t) = U$$

$$i(t) = I$$



$$u(t) = U_{peak} \cos(\omega t - \alpha)$$

$$i(t) = I_{peak} \cos(\omega t - \beta)$$

$$\omega = 2\pi f$$

RMS = Root-Mean-Square

$$I_{RMS} = \sqrt{\frac{1}{T} \int_0^T i(t)^2 dt} = \frac{I_{peak}}{\sqrt{2}}$$

Only for sinusoidal waveforms

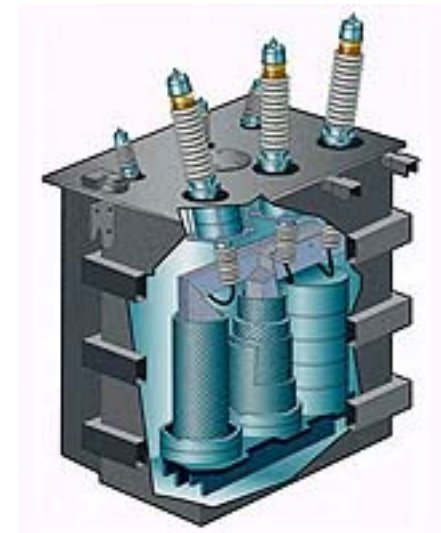
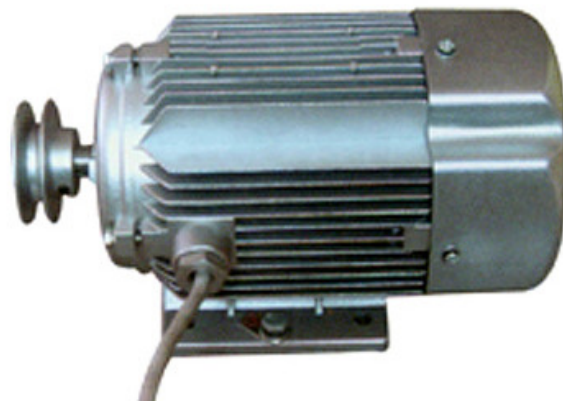


# Why is AC used?

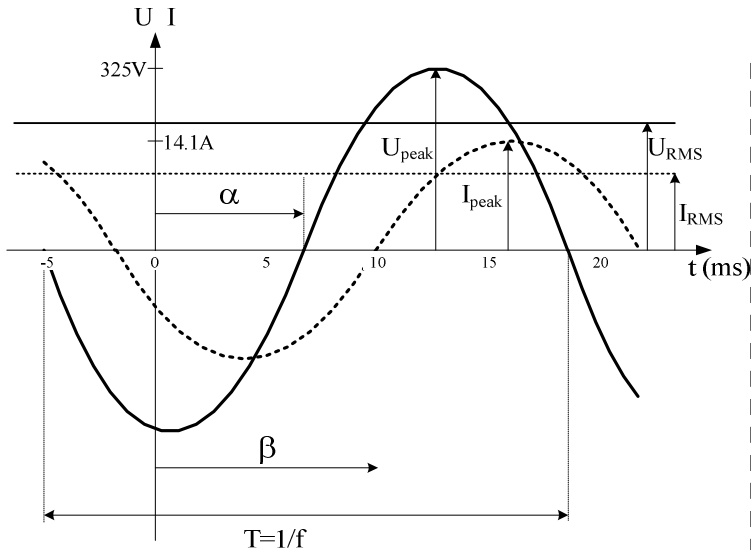
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The **two main** factors that formed the power system

- Transformer (only works on AC)
- Robust and cheap motor (rotating flux)



# Alternating Current (AC)

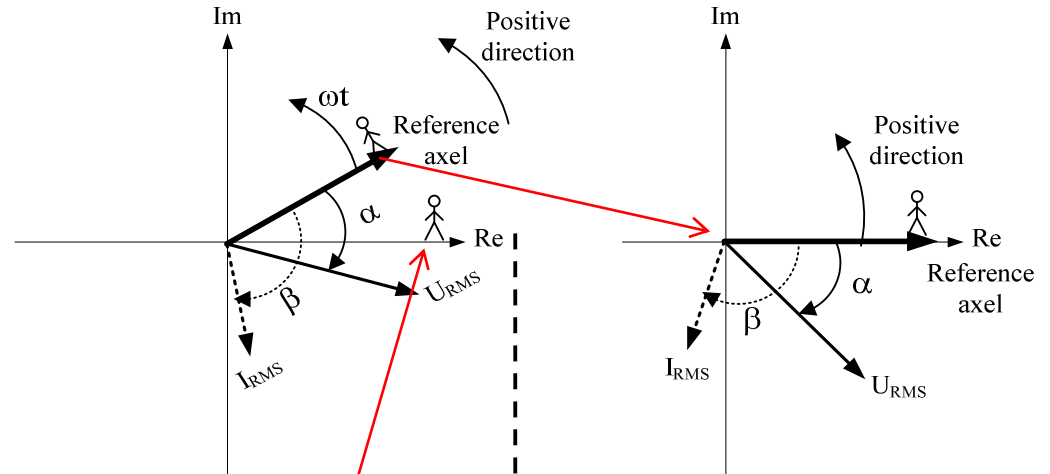


$$u(t) = U_{peak} \cos(\omega t - \alpha)$$

$$i(t) = I_{peak} \cos(\omega t - \beta)$$

$$\omega = 2\pi f$$

Express the sinusoidal voltage and current as complex rotating phasors and use RMS values for the amplitude



$$u(t) = \sqrt{2} \operatorname{Re}\{U_{RMS} e^{j(\omega t - \alpha)}\} \Rightarrow$$

$$u(t) = \sqrt{2} \operatorname{Re}\left\{ \underbrace{U_{RMS} e^{j(-\alpha)}}_{\underline{U}} e^{j\omega t} \right\}$$

$$i(t) = \sqrt{2} \operatorname{Re}\{I_{RMS} e^{j(\omega t - \beta)}\} \Rightarrow$$

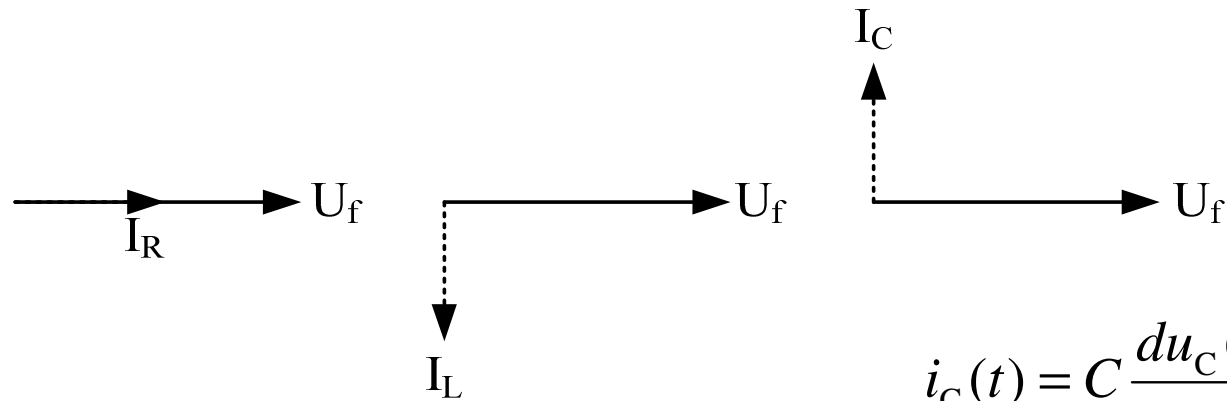
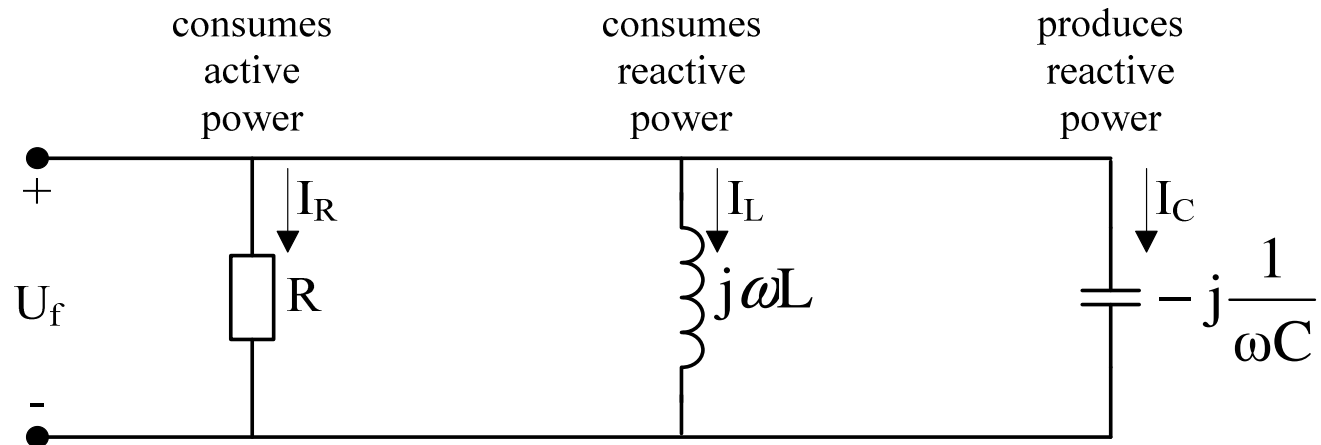
$$i(t) = \sqrt{2} \operatorname{Re}\left\{ \underbrace{I_{RMS} e^{j(-\beta)}}_{\underline{I}} e^{j\omega t} \right\}$$

Since all phasors are rotating with the same speed, we select one as the reference and observe all others relative to this one. This gives that the rotation disappears and the voltage and currents can be expressed as complex number (constant)

$$\underline{U} = U_{RMS} \angle \alpha$$

$$\underline{I} = I_{RMS} \angle \beta$$

# Impedance



$$u_R(t) = R i_R(t)$$

$$\underline{U}_R = R \underline{I}_R$$

$$u_L(t) = L \frac{di_L(t)}{dt}$$

$$\underline{U}_L = j\omega L \underline{I}_L = jX_L \underline{I}_L$$

$$X_L = \omega L$$

$$i_C(t) = C \frac{du_C(t)}{dt}$$

$$\underline{U}_C = -j \frac{1}{\omega C} \underline{I}_C = -jX_C \underline{I}_L$$

$$X_C = \frac{1}{\omega C}$$



# Reactive power (Q) flow – What is reactive power?

A mathematical description of the phase shift between voltage and current

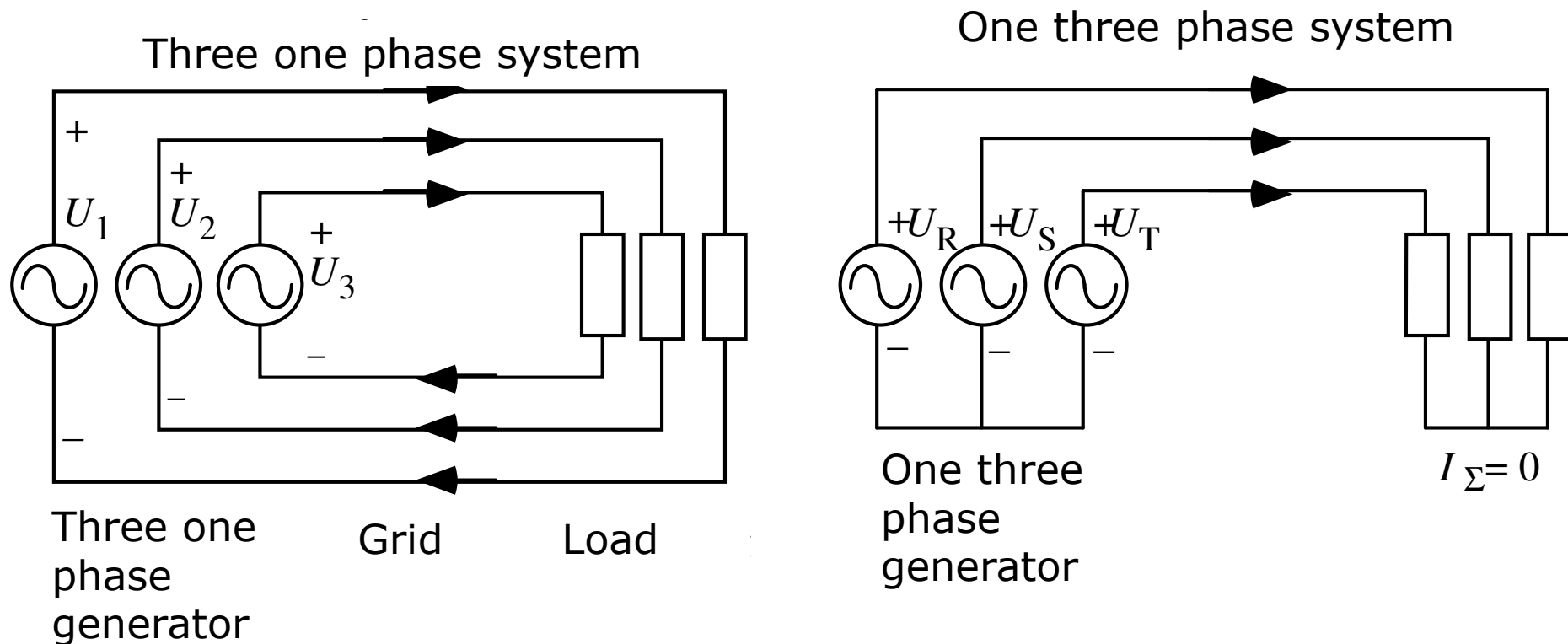
## Reactive power (Q) flow – Why care?

Due to the presence of the reactive power, the system cannot be used up to its thermal limit and its voltage variation limits



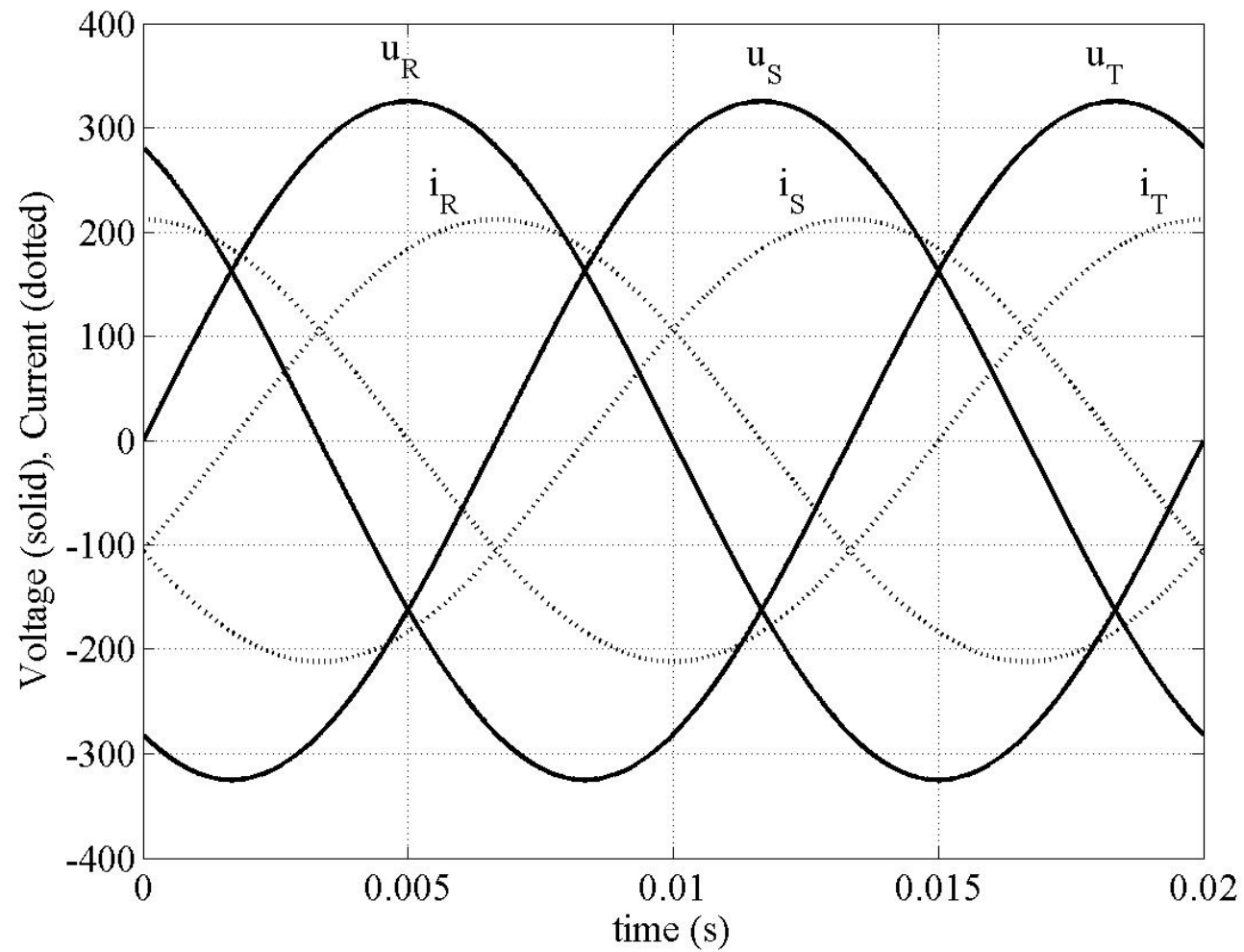
*Need for reactive power compensation for better utilization of the system*

# Why three phase system?

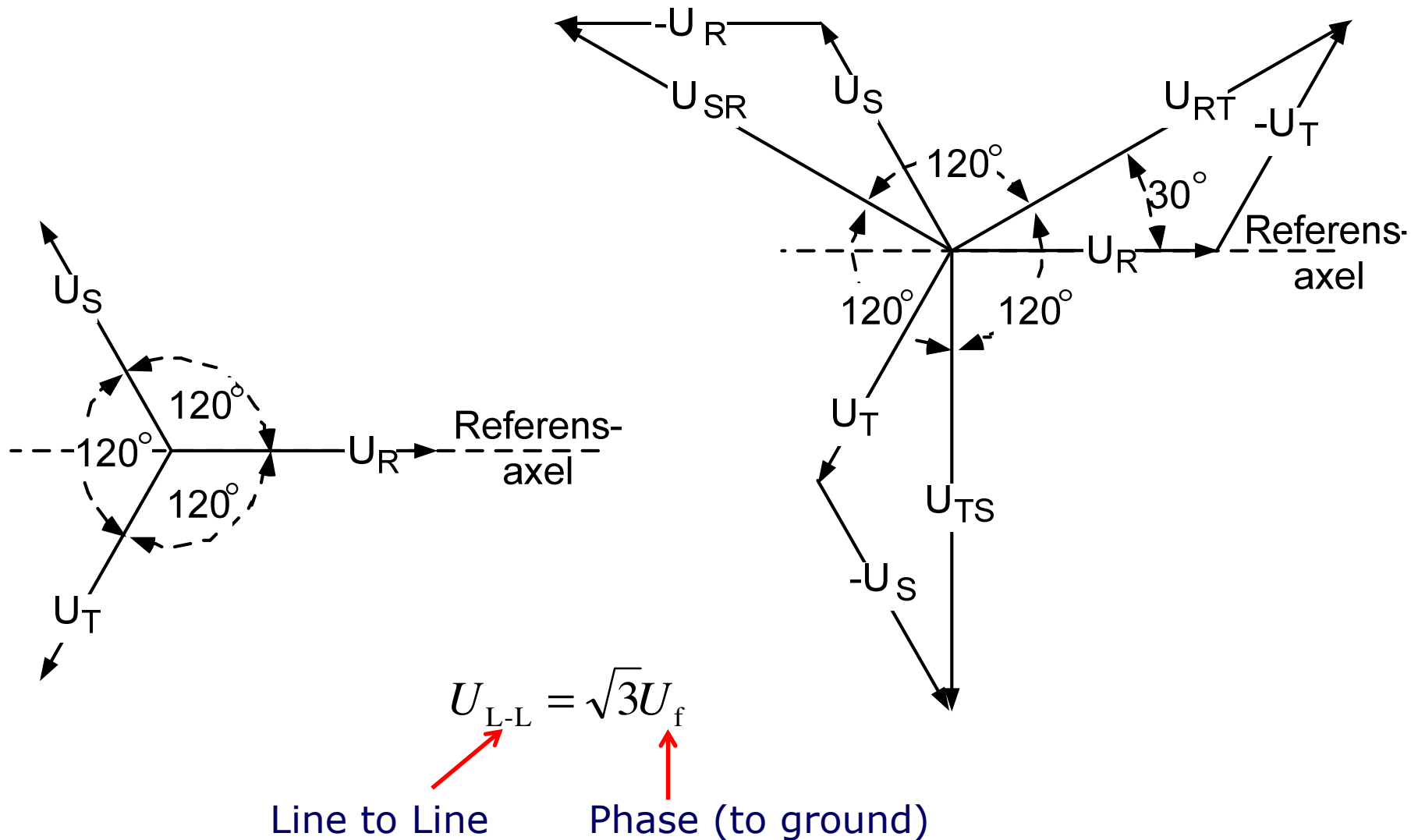


The lowest number of phases that could create a rotating electric field

# Three phase voltage and current



# Line-to-line phasors for the voltages



## Power – Rate of energy flow [W]

$$u(t) = \sqrt{2}U_{RMS} \cos(\omega t)$$

$$i(t) = \sqrt{2}I_{RMS} \cos(\omega t - \varphi)$$

Angle between voltage and current

$$\varphi = \beta - \alpha$$

Single phase

Three phase

$$p(t) = u(t)i(t)dt \quad \leftarrow \text{Instantaneous power} \rightarrow$$

$$p(t) = u_R(t)i_R(t) + u_S(t)i_S(t) + u_T(t)i_T(t)$$

$$P = \frac{1}{T} \int_0^T u(t)i(t)dt \quad \leftarrow \text{average} \rightarrow$$

$$P = \frac{1}{T} \int_0^T \{u_R(t)i_R(t) + u_S(t)i_S(t) + u_T(t)i_T(t)\}dt$$

Apparent power

$$S = \underline{U}_{RMS} \underline{I}_{RMS}^* = P + jQ \quad [\text{VA}]$$

$$S = 3\underline{U}_{RMS} \underline{I}_{RMS}^* = \sqrt{3}\underline{U}_{L-L,RMS} \underline{I}_{RMS}^* = P + jQ$$

Active power

$$P = |\underline{U}_{RMS}| |\underline{I}_{RMS}| \cos \varphi \quad [\text{W}]$$

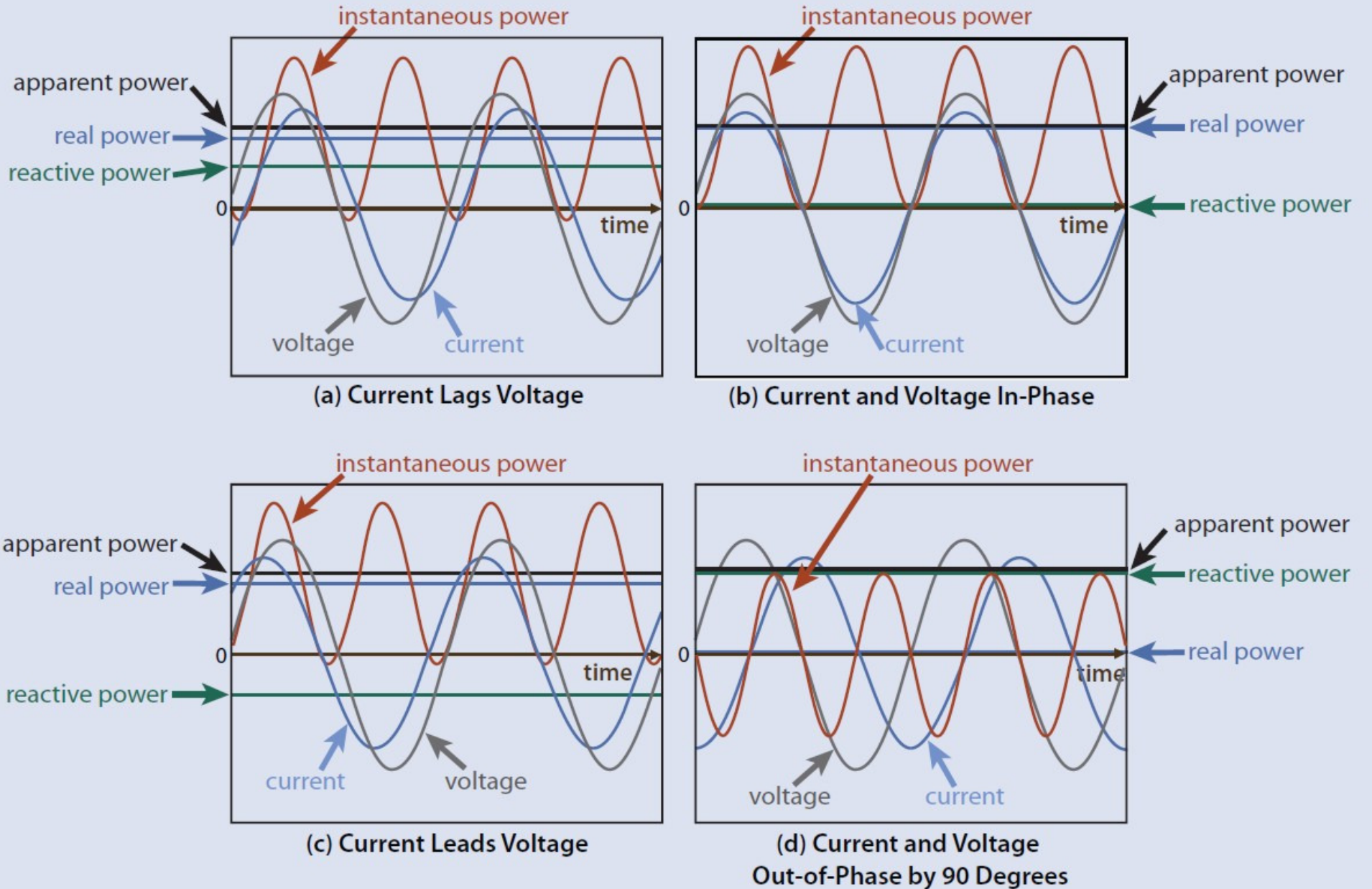
$$P = 3|\underline{U}_{RMS}| |\underline{I}_{RMS}| \cos \varphi = \sqrt{3}|\underline{U}_{L-L,RMS}| |\underline{I}_{RMS}| \cos \varphi$$

Reactive power

$$Q = |\underline{U}_{RMS}| |\underline{I}_{RMS}| \sin \varphi \quad [\text{VAr}]$$

$$Q = 3|\underline{U}_{RMS}| |\underline{I}_{RMS}| \sin \varphi = \sqrt{3}|\underline{U}_{L-L,RMS}| |\underline{I}_{RMS}| \sin \varphi$$

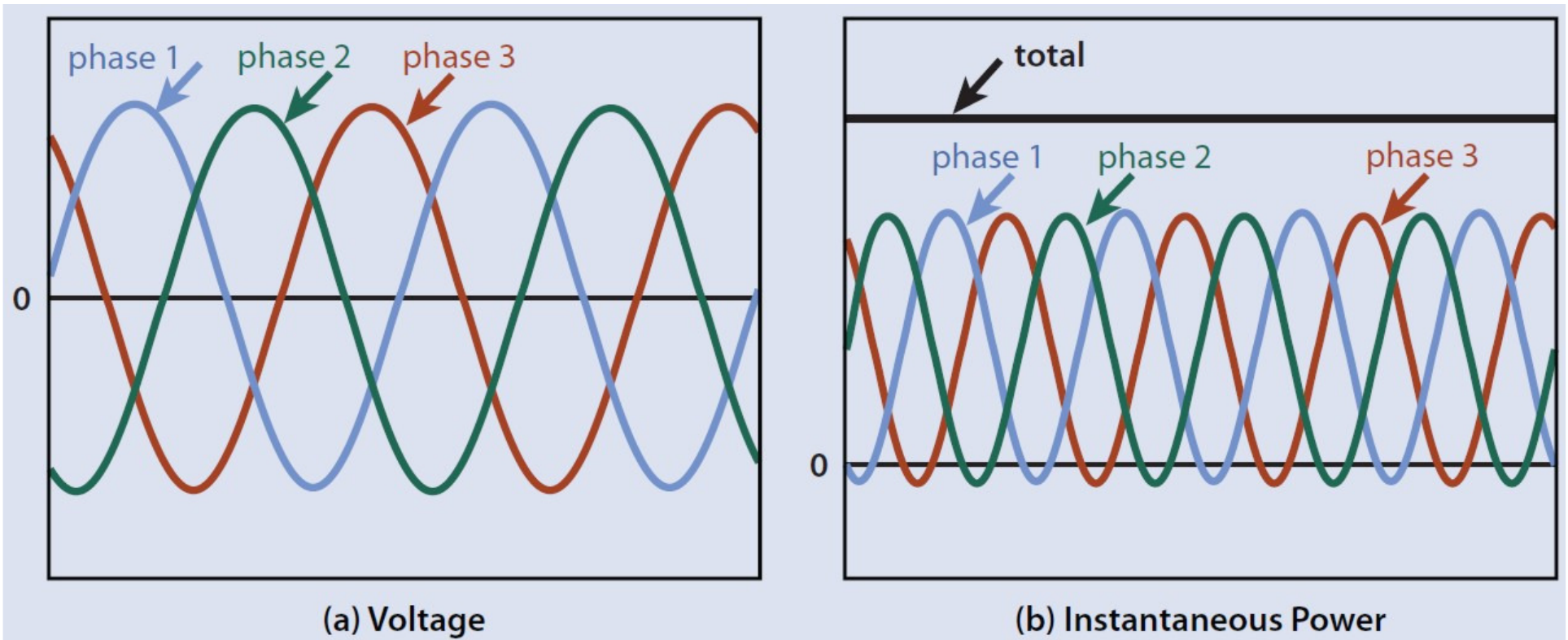
# Power – Rate of energy flow [W]



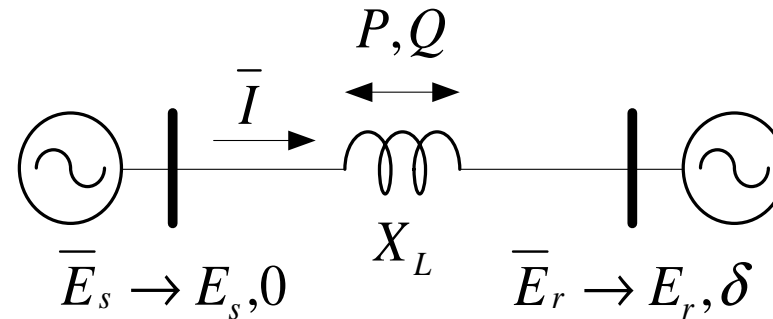


# Power – Rate of energy flow [W]

## 3-phase Power [W]



# Power flow



Active/reactive power at sending end  $E_s$

Active/reactive power at receiving end  $E_r$

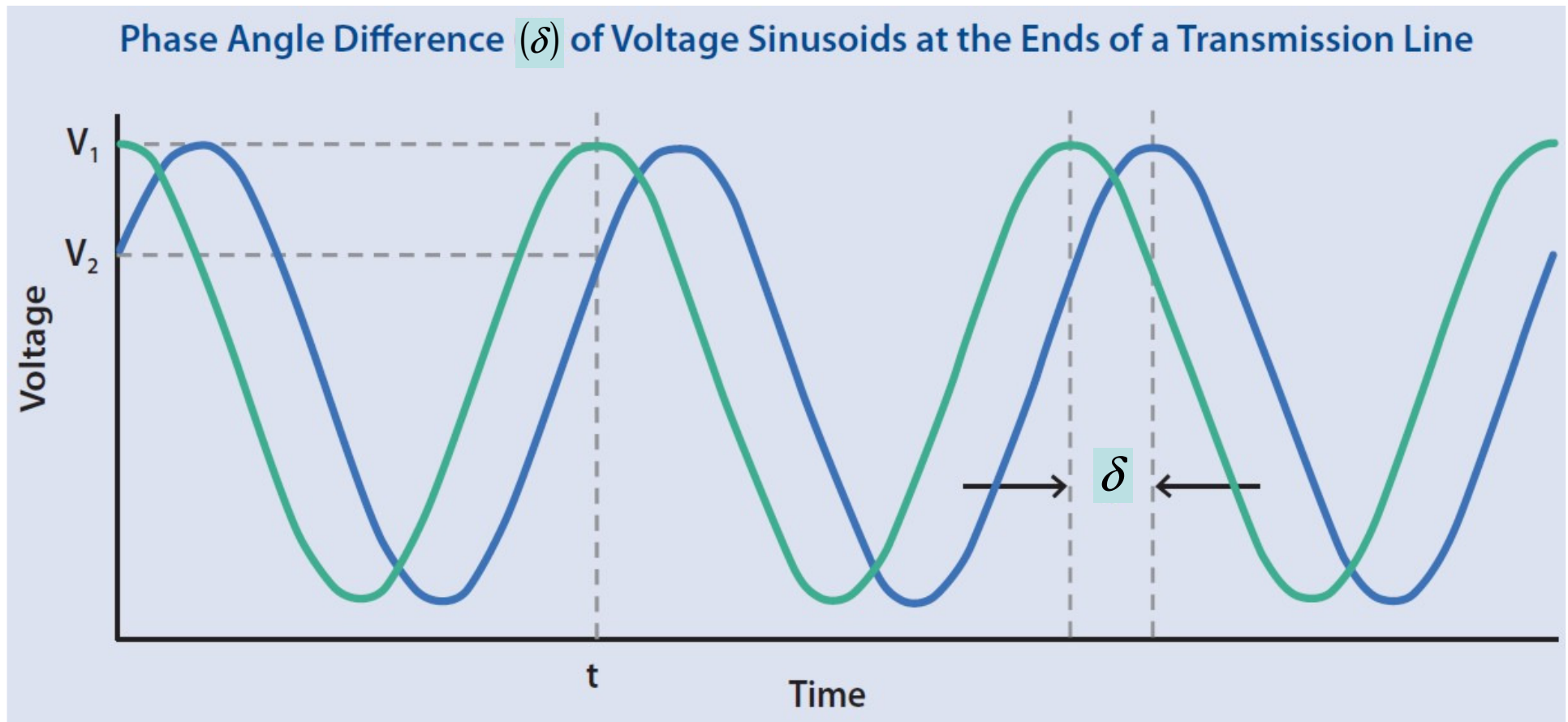
$$P_s = \text{real}(\bar{E}_s \bar{I}^*) = E_s I_p = \frac{E_s E_r \sin \delta}{X_L}$$

$$P_r = \text{real}(\bar{E}_r \bar{I}^*) = \frac{E_r E_s \sin \delta}{X_L}$$

$$Q_s = \text{imag}(\bar{E}_s \bar{I}^*) = E_s I_q = \frac{E_s (E_s - E_r \cos \delta)}{X_L}$$

$$Q_r = \text{imag}(\bar{E}_r \bar{I}^*) = -\frac{E_r (E_r - E_s \cos \delta)}{X_L}$$

# Voltages at the ends of a transmission line (same phase)



$s = 1$  (sending end)  
 $r = 2$  (receiving end)

s = 1 (sending end)  
r = 2 (receiving end)

## Power flow

$$\bar{I} = \frac{\bar{E}_1 - \bar{E}_2}{jX} = \frac{E_1 \sin \delta}{X} + j \frac{E_2 - E_1 \cos \delta}{X} = I_{p2} - jI_{q2}$$

Complex power to  $E_2$ :

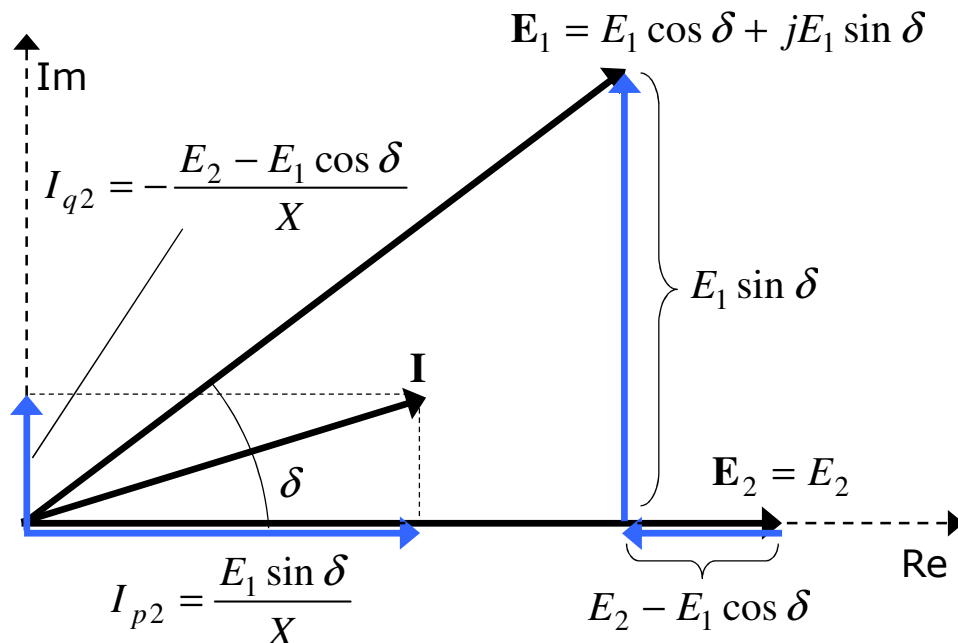
$$\bar{S}_2 = \bar{E}_2 \bar{I}^* = E_2 (I_{p2} + jI_{q2}) = P_2 + jQ_2$$

Active/reactive power to

$$E_2:$$

$$P_2 = E_2 I_{p2} = \frac{E_2 E_1 \sin \delta}{X}$$

$$Q_2 = E_2 I_{q2} = -\frac{E_2 (E_2 - E_1 \cos \delta)}{X}$$



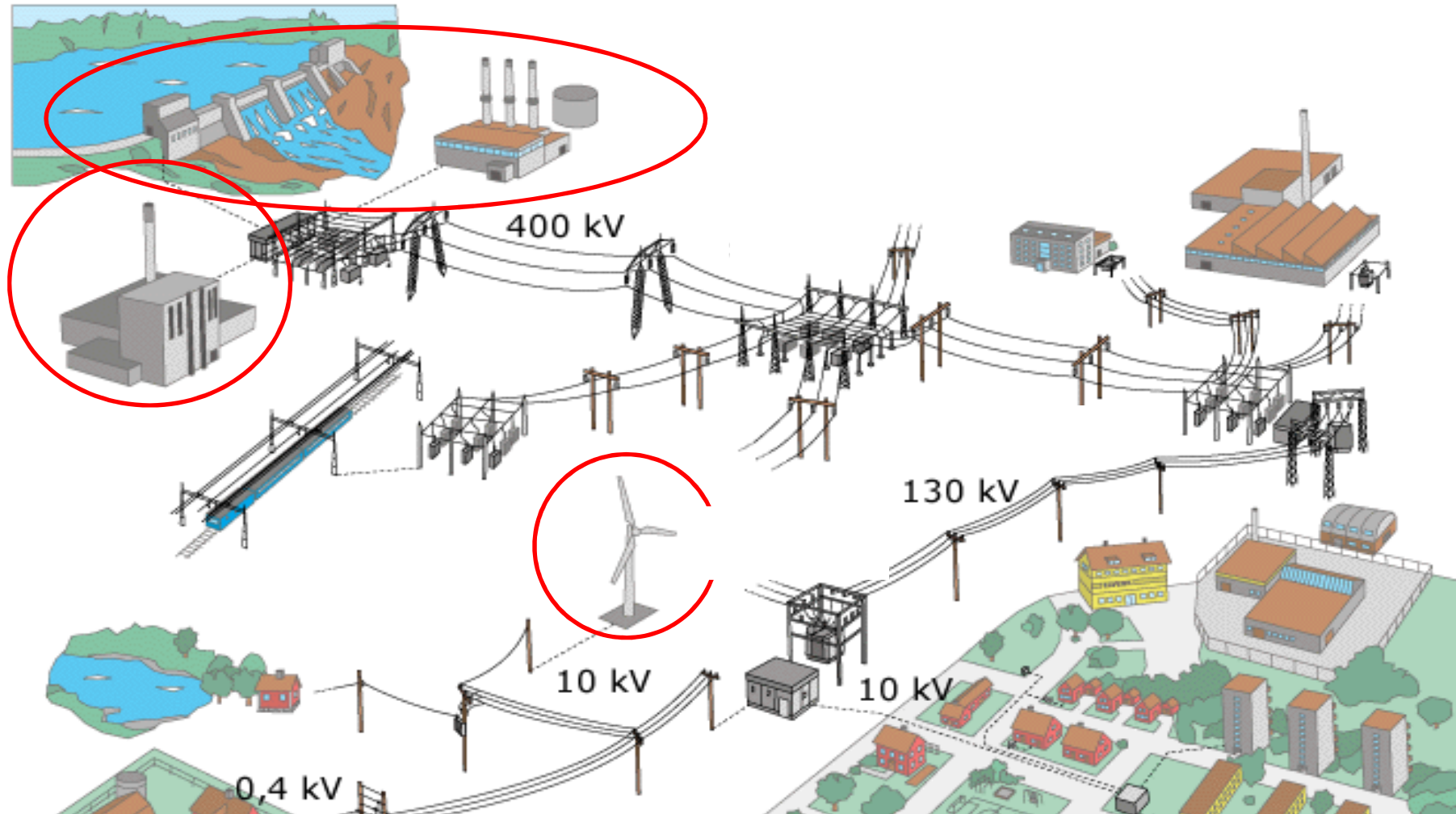
Active power from  $E_1$  to  $E_2$  :

$$P = P_1 = P_2 = \frac{E_2 E_1 \sin \delta}{X}$$

Reactive power consumption of the transmission line:

$$\Delta Q = Q_1 - Q_2 = \frac{1}{X} (E_1^2 + E_2^2 - 2E_1 E_2 \cos \delta) = \frac{E_L^2}{X}$$

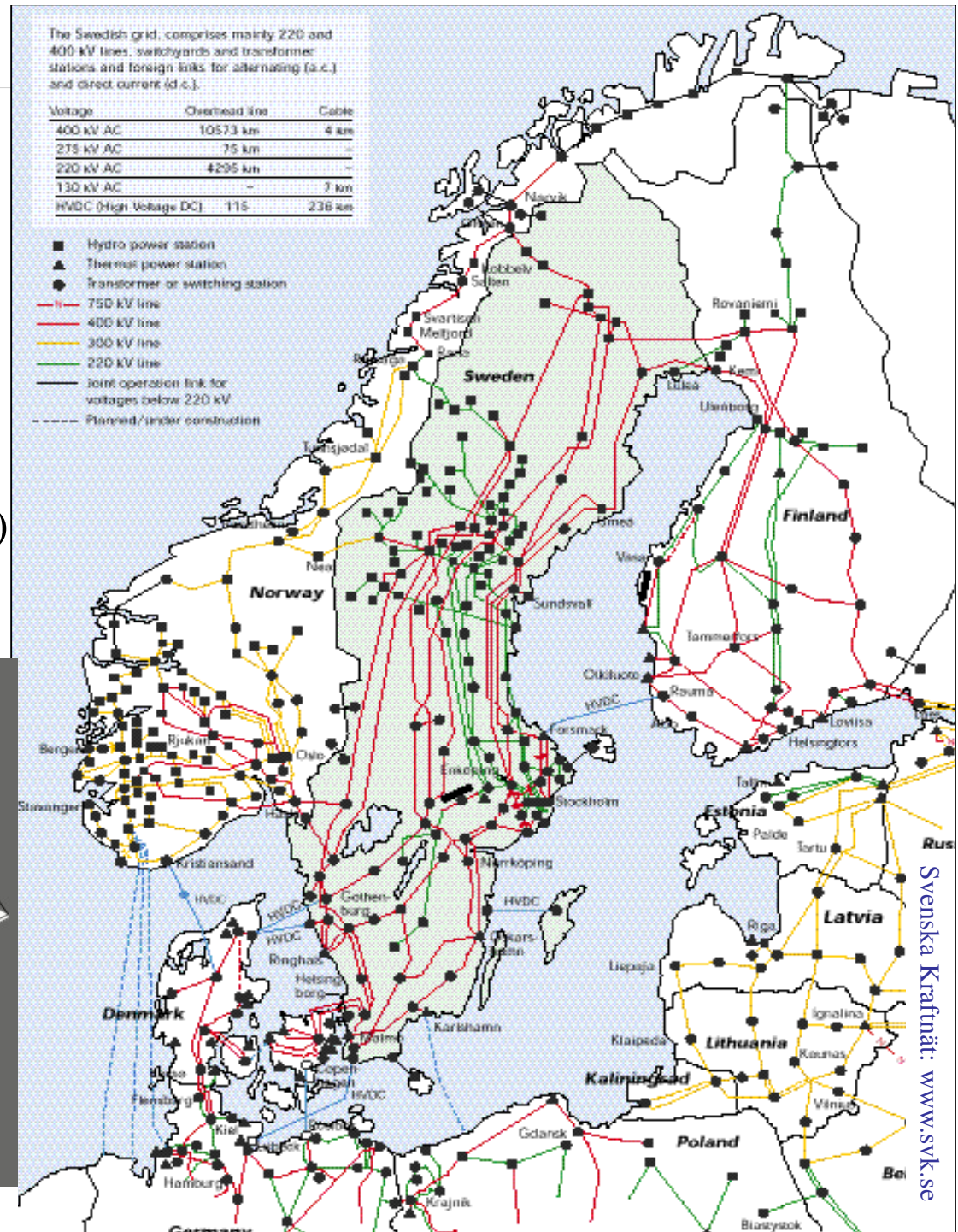
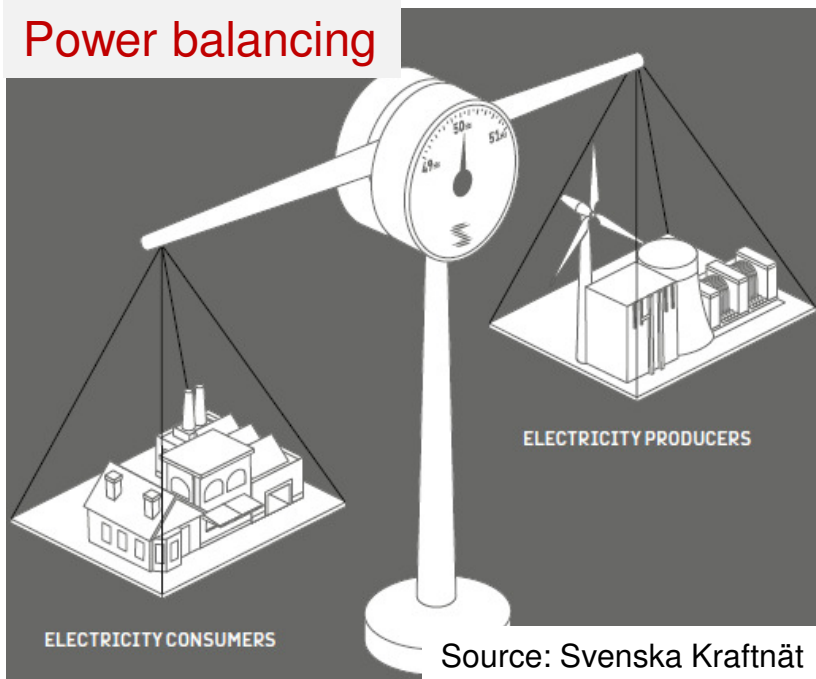
# Structure of the Electric Power System



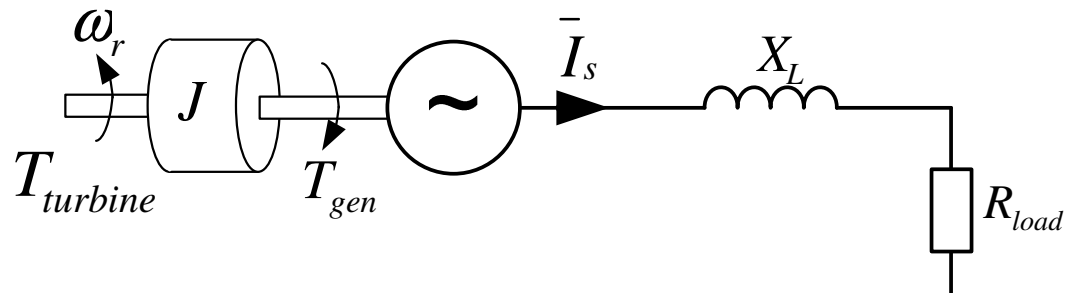


- Transmission 400, 220 kV
- Regional 130 kV
- Distribution 70, 40, 30, 20, 10 kV
- Local 400 V (Industry 10-130 kV)

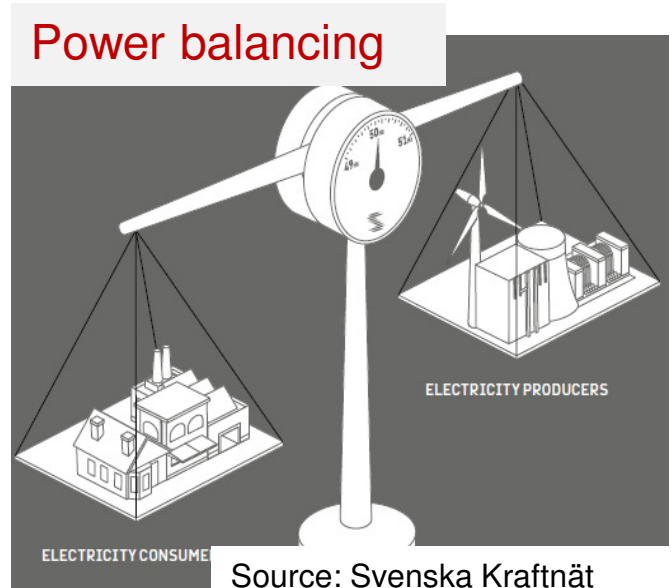
**Power balancing**



# What happens if the turbine power does not match the load power?

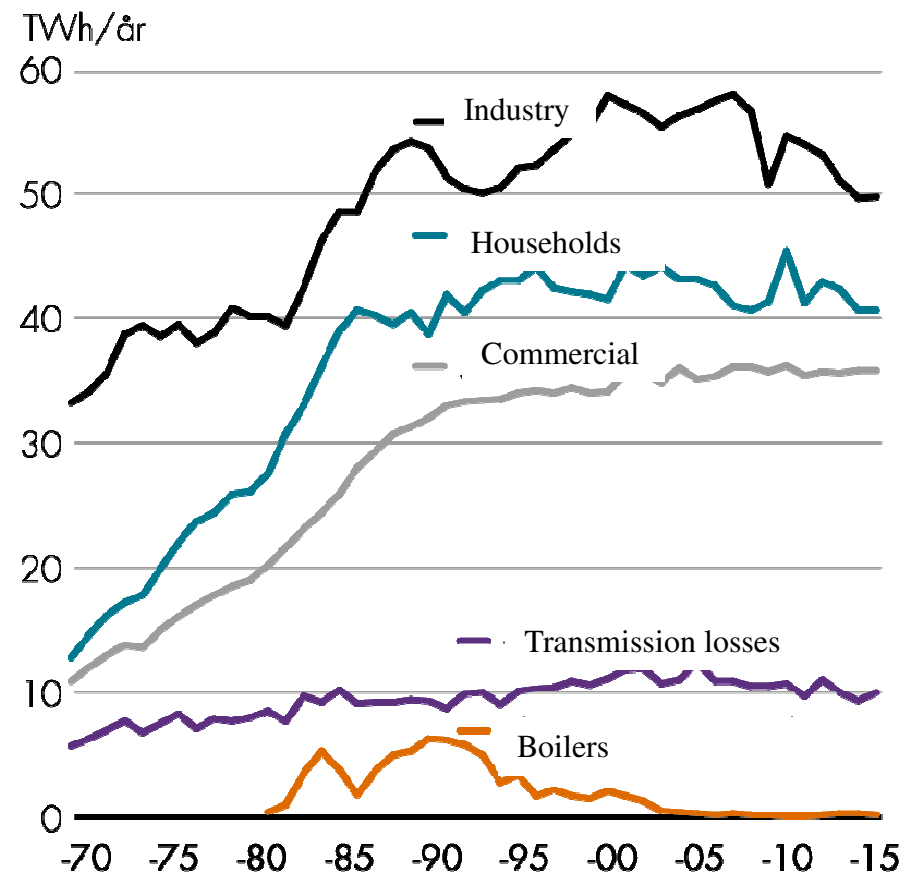


$$\left. \begin{aligned}
 J \frac{d\omega_r}{dt} &= T_{turbine} - T_{gen} \\
 P_{turbine} &= \omega_r T_{turbine} \\
 P_{gen} &= \omega_r T_{gen} \\
 P_{load} &\approx P_{gen} \\
 \omega_r &= \frac{2\pi f_{grid}}{n_p}
 \end{aligned} \right\} \Rightarrow J \frac{4\pi^2}{n_p^2} \frac{df_{grid}}{dt} = \frac{P_{turbine} - P_{gen}}{f_{grid}}$$





# Electric energy consumption in Sweden divided on different consumers 1970–2015

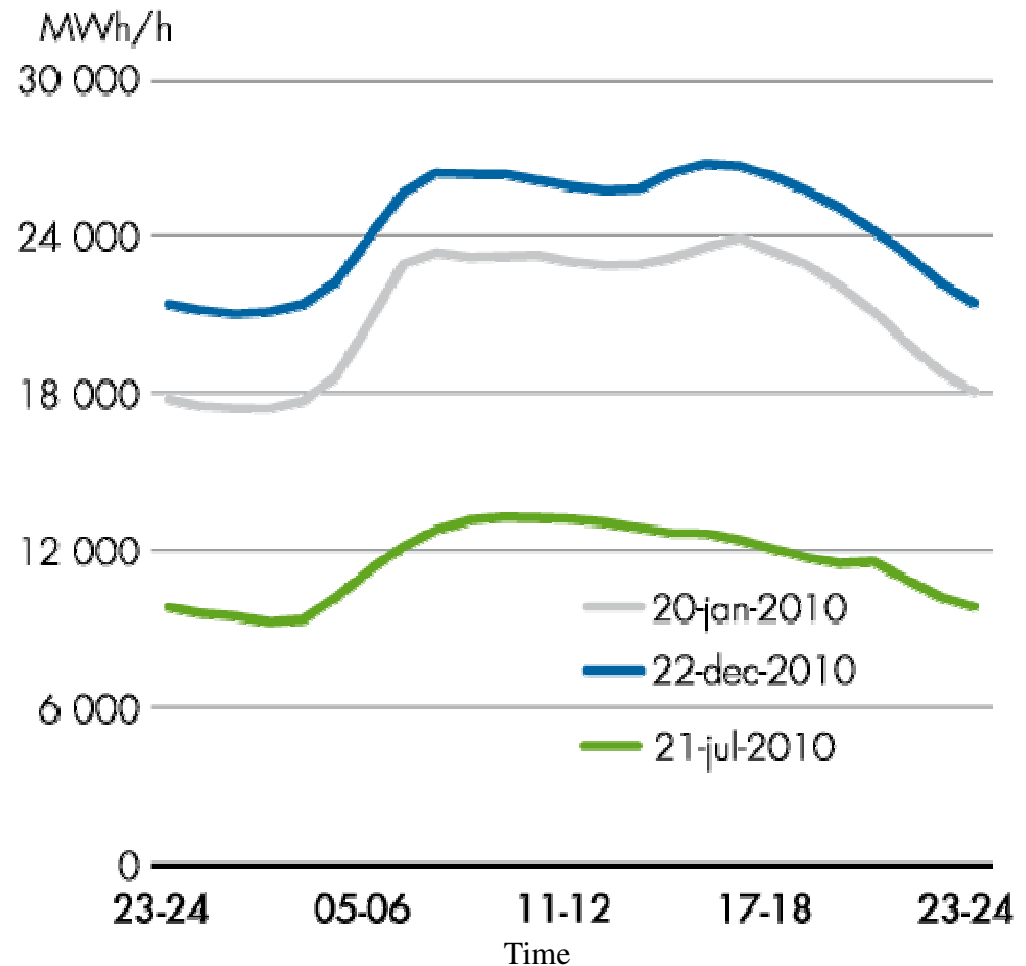


Källa: SCB

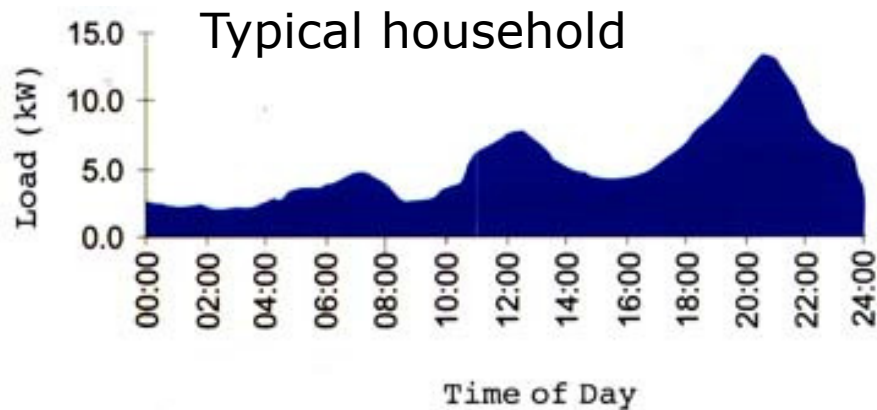
## Profile over the electric energy consumption in Sweden for a typical summer day, winter day and the highest consumption day 22th of December 2010

On the 23rd of  
February 2011  
Sweden used  
**26 000 MW**  
between 08-09

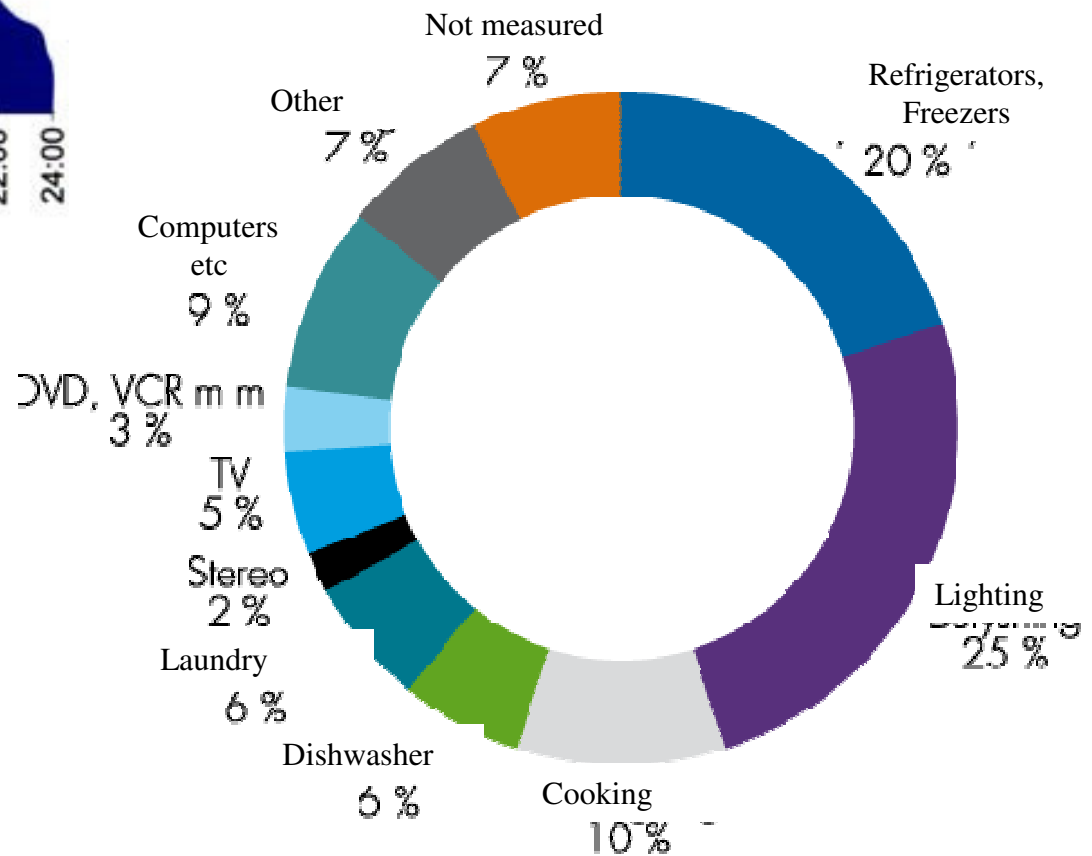
The consumption is higher in winter time in the Nordic countries, but in warm countries it is opposite



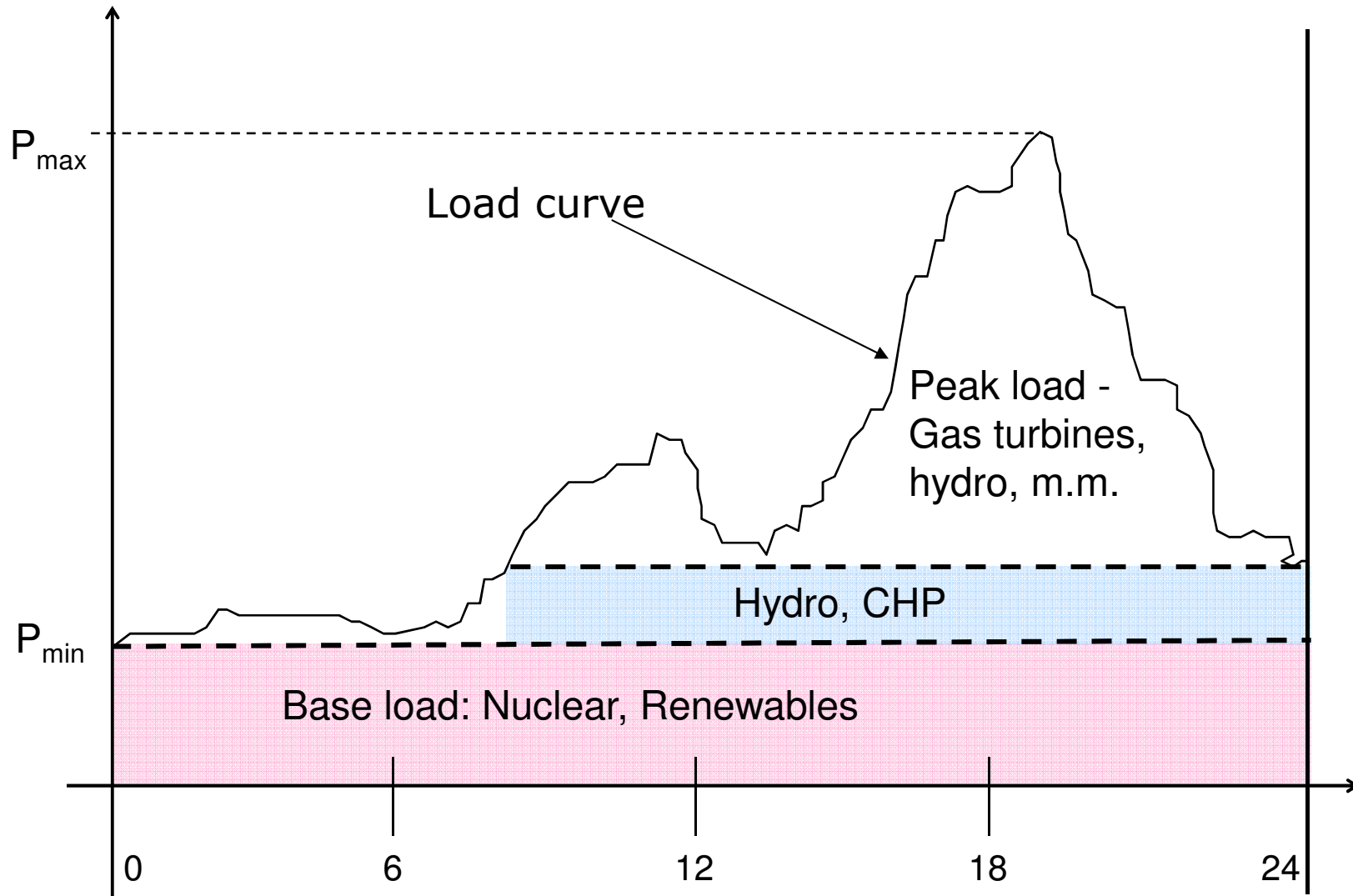
# Electric energy consumption for households in Sweden (investigated 2007)



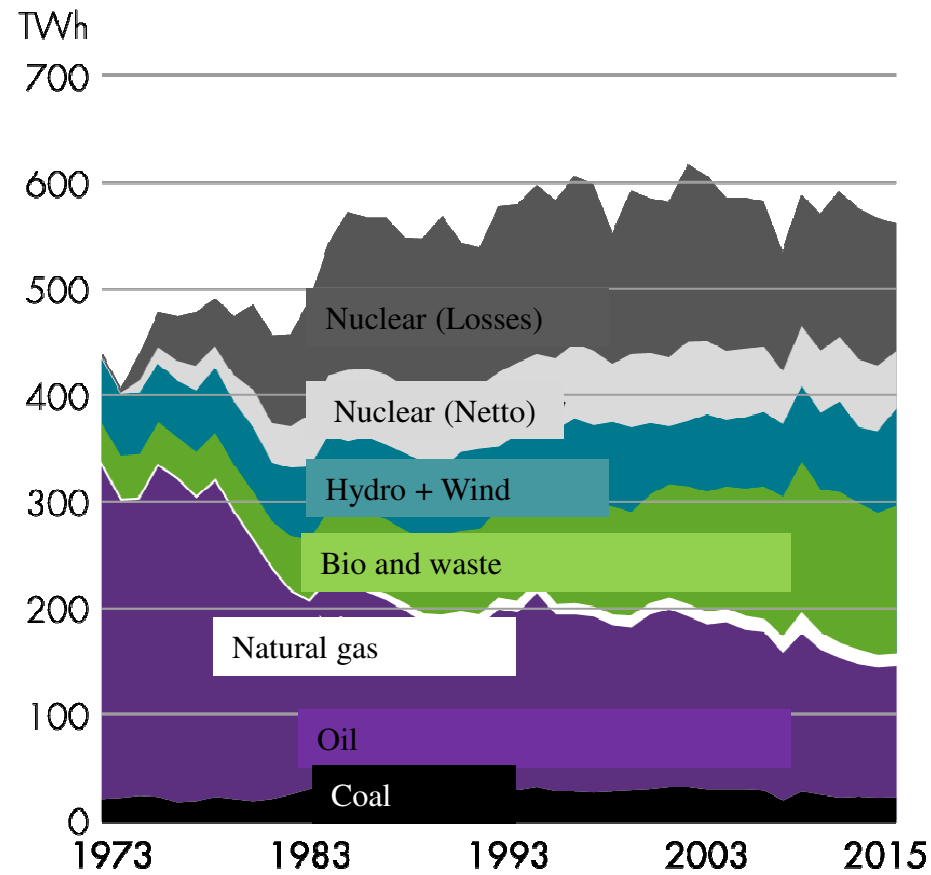
The consumption is higher in winter time in the Nordic countries, but in warm countries it is opposite



# Production planning



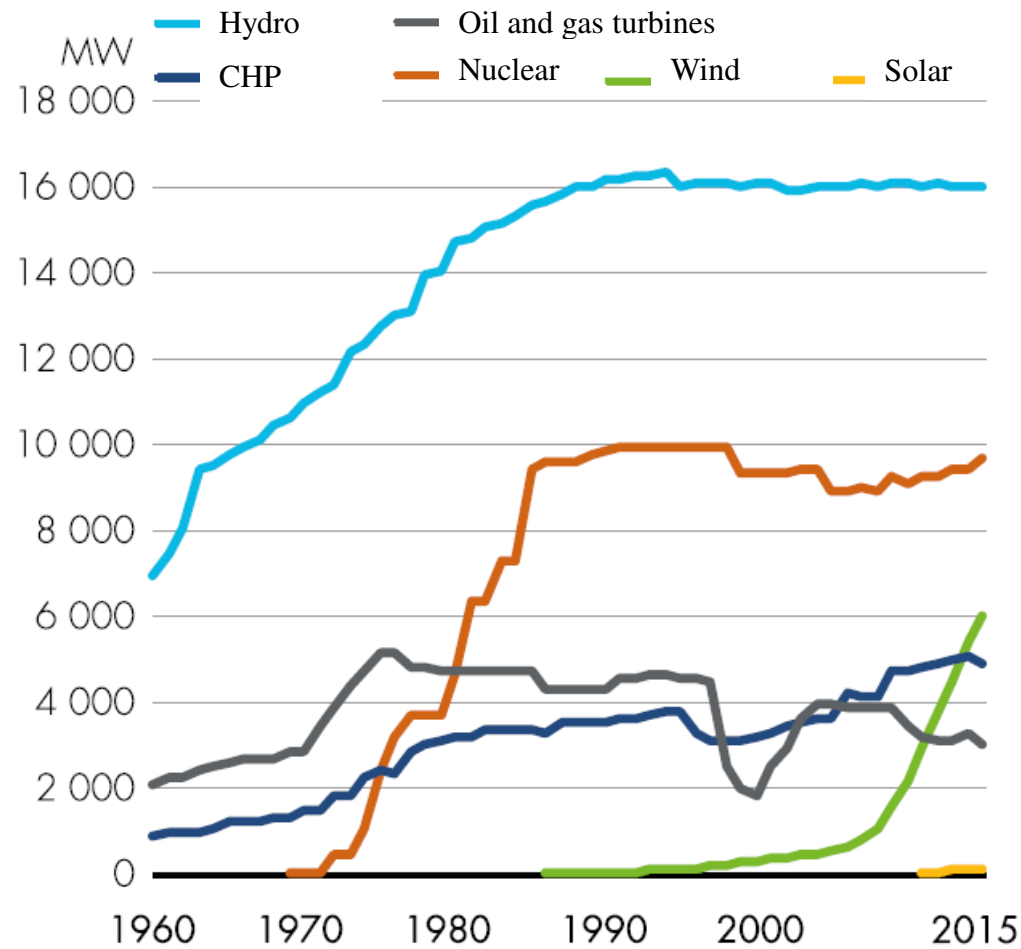
# Total input energy to Sweden 1973–2015



Källa: SCB

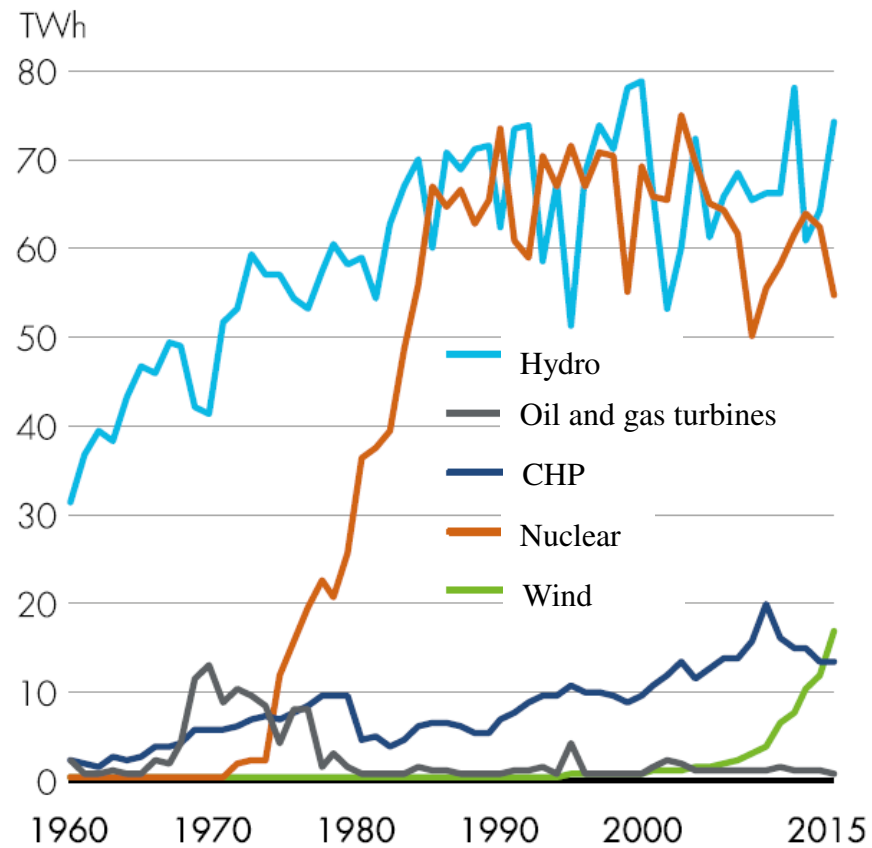
Elåret 2015

# Installed peak power in Sweden, MWe1



Source: Svensk Energi

# Electricity production in Sweden, TWh<sub>el</sub>



Source: *Svensk Energi*



# Solar Plant

Göteborg

Latitude  $57.7^\circ$

200 m<sup>2</sup> of solar cells

Statistical cloudiness

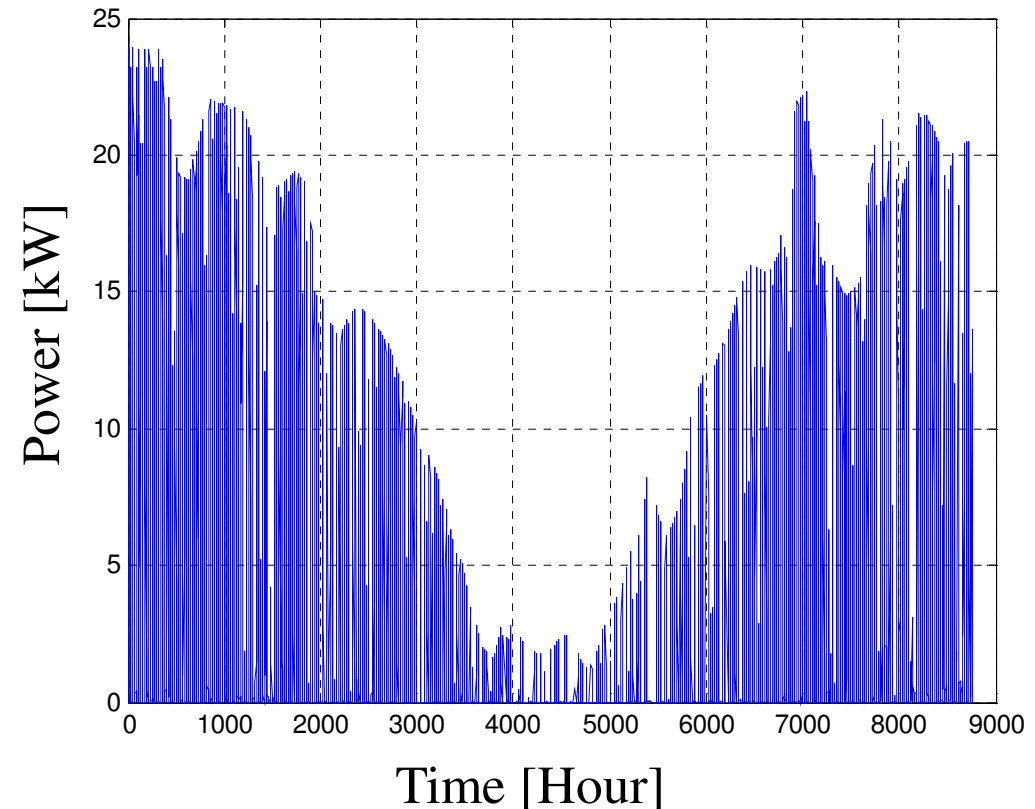
Sun tracking

Efficiency:

MPP 0.95

Power electronics 0.95

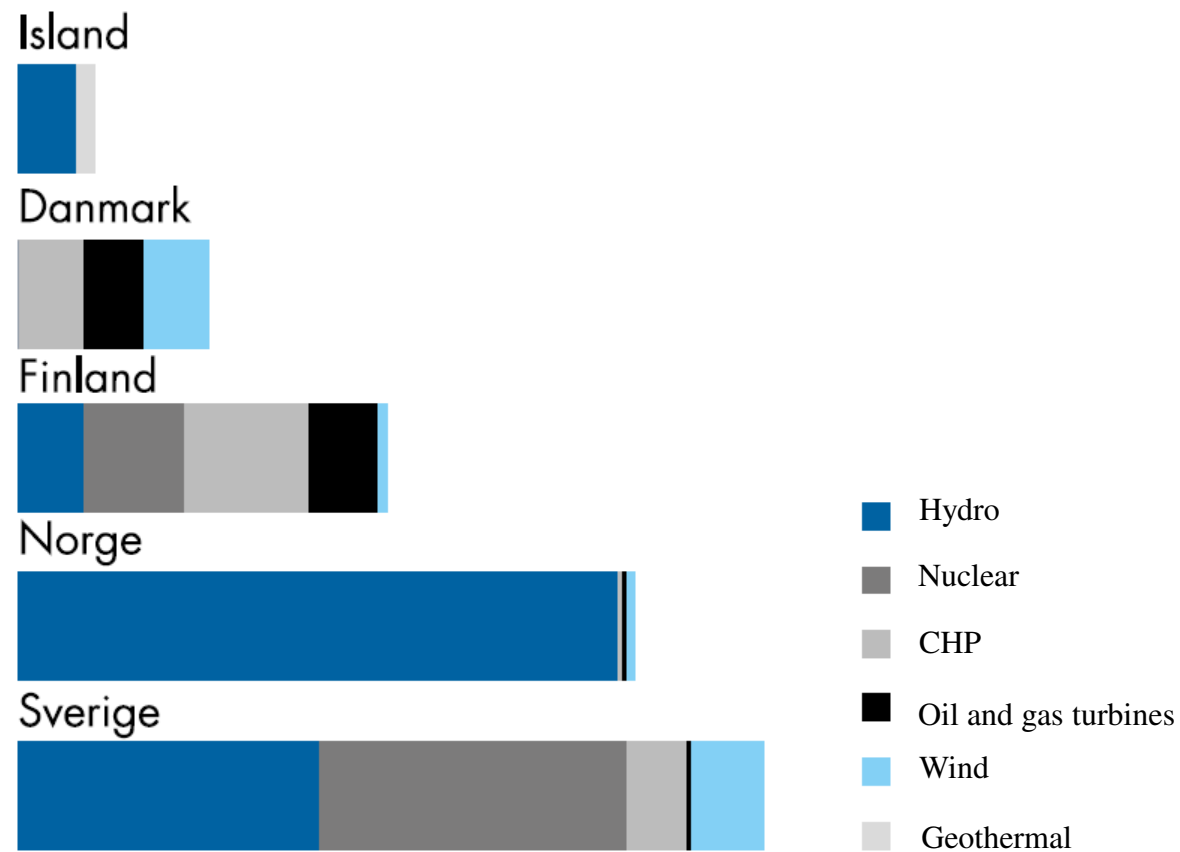
Solar cells 0.15



Integrated power during 1 year

**24 000 kWh**

# Normalized electric production mix for the Nordic countries



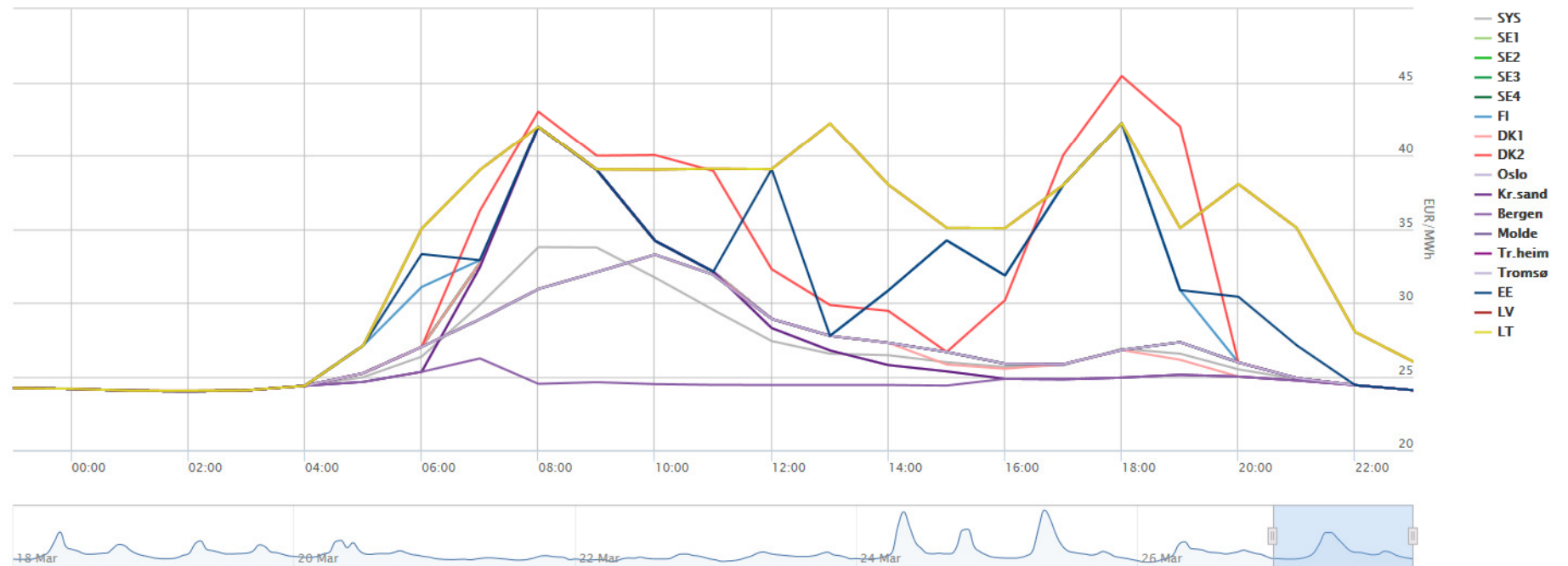
Source: *Svensk Energi*

# Spot market price for 2015-03-27

ELSPOT PRICES [Elsport prices](#)

Changes in the Norwegian bidding areas can affect which geographical area the city references refer to. Please see the [area change log pdf](#).

Zoom



**The End**

*Do you have any questions?*